
Constraint Imperative Programming with Turtle

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Introduction

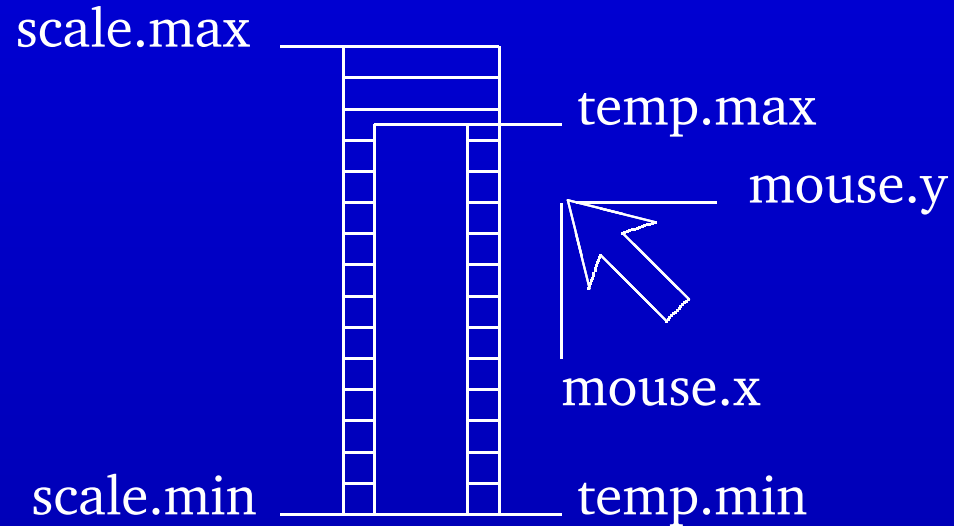
- Constraint imperative programming
- Language design
- CIP with Turtle: an example
- Implementation
- Presentation

Constraint Imperative Programming

Constraint Imperative Programming

- Imperative programming is statement oriented
- Constraint programming is declarative
- Constraint imperative programming (CIP) combines these programming paradigms
- Goal: combine advantages of both

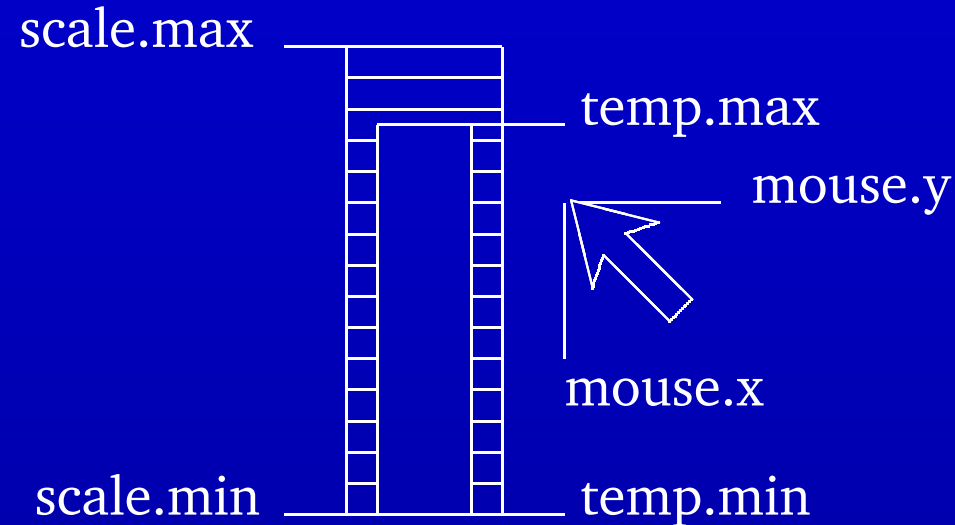
Example



- Control temperature column with mouse

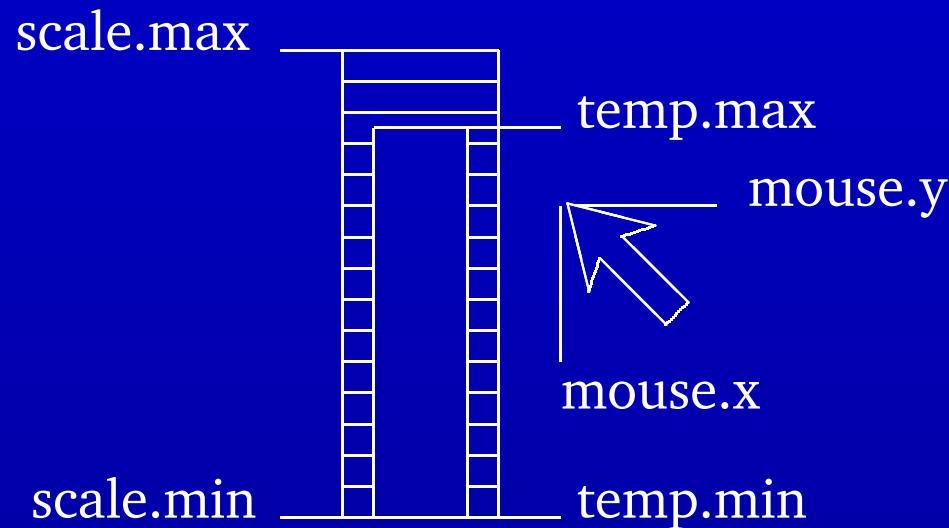
Imperative Approach

```
while mouse.pressed do
  var y: int;
  y ← mouse.y
  if y > scale.max then
    y ← scale.max;
  else
    if y < scale.min then
      y ← scale.min;
    end;
  end;
  temp.max ← y
end;
```



Constraint Imperative Approach

```
require  $temp.max \leq scale.max$ ;  
require  $temp.max \geq scale.min$ ;  
while mouse.pressed prefer  $temp.max = mouse.y$ ;
```



Language Design

Base Language

- Variables and assignments
- Conditionals and loops
- Subprograms
- Higher-order functions
- Lists, arrays and algebraic data types
- Parameterized modules

Imperative Program

```
module main;
```

```
import io, listsort<string>, compare;
```

```
fun main (argv: list of string): int
```

```
  var l: list of string := io.get (io.open ("main.t"));
```

```
  io.put (listsort.sort (l, compare.cmp));
```

```
  return 0;
```

```
end;
```

Constraint Extensions

- Constrainable variables
- Constraint statements
- User-defined constraints
- Constraint solvers

Constrainable Variables

```
var x: !real := var 0;
```

- Values of constrainable variables are determined by constraints
- Are declared with special types
- Contain *variable objects* encapsulating their values (constructed by **var** expressions)
- Can thereby be shared between data structures

Constraint Statements (1)

```
require x = 2 in
  io.put (!x);    // prints "2"
end;
```

- Constraint conjunctions are added to the stores of responsible constraint solvers
- Constraints are solved (variables are assigned)
- Statements in the statement body are executed
- Constraints are removed at the end of the body

Constraint Statements (2)

```
require x = 2 and y >= x and y = 0 : weak in
  io.put (!y);    // prints "2"
end;
```

- Individual constraints can have different priorities
- Constraints can form *constraint hierarchies*
- Less important constraints may be violated in order to satisfy more important ones
- Constraint solvers minimize the resulting error

User-defined Constraints (1)

```
constraint between (v: !int, min: int, max: int)
  require v >= min and v <= max;
end;
```

- User-defined constraints make constraint conjunctions reusable
- Like primitive constraints (e.g. relations like \leq), can be used in constraint statements
- Parameters can be constrainable variables or values

User-defined Constraints (2)

```
constraint all_different (l: list of !int)
  while (tl l <> null) do
    var ll: list of !int := tl l;
    while (ll <> null) do
      require hd l <> hd ll;
      ll := tl ll;
    end;
    l := tl l;
  end;
end;

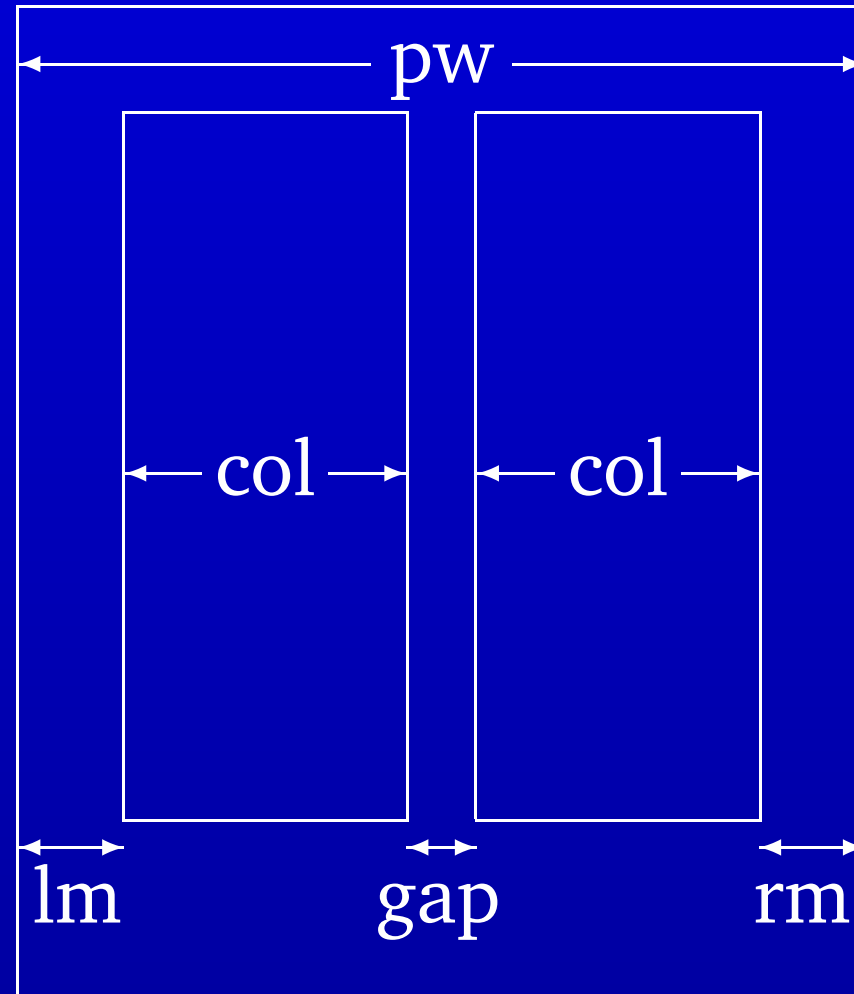
...
require all_different ([a, b, c]);
```

Constraint Solvers

- Manage the set of active constraints in constraint stores
- Check the satisfiability of the stores
- Calculate assignments for constrainable variables
- Raise exceptions when constraint conjunctions are not satisfiable
- New solvers can easily be integrated

CIP with Turtle: *An Example*

Example – Layout Calculation



$$pw = lm + 2col + gap + rm$$

Example Program

```
module layout;
import io;
fun main (args: list of string): int
  var lm: !real := var 0.0;
  var rm: !real := var 0.0;
  var gap: !real := var 0.0;
  var pw: !real := var 0.0;
  var col: !real := var 0.0;
  require lm = 2.0 and rm = 2.0 and pw = 21.0 and
    gap >= 0.5 and gap <= 2.0 and gap = 0.5 : medium and
    col <= 7.0 : strong and gap + lm + 2.0 * col + rm = pw in
    io.put ("lm="); io.put (!lm); io.nl ();
    io.put ("rm="); io.put (!rm); io.nl ();
    io.put ("gap="); io.put (!gap); io.nl ();
    io.put ("pw="); io.put (!pw); io.nl ();
    io.put ("col="); io.put (!col); io.nl ();
  end;
return 0; end;
```

Layout Calculation

- Constraints for lm , rm und pw have highest priority and must get satisfied:
 $lm = 2.0 \wedge rm = 2.0 \wedge pw = 21.0$
- gap may be at most 2.0: $gap = 2.0$
- col has to be enlarged in order to fulfill the main constraint: $col = 7.5$
- Priority of $gap = 0.5$ is weaker than $col \leq 7.0$, so the former constraint is violated
- Since $gap \leq 2.0$ is required, the constraint on col is violated, too

Implementation

Implementation

- Compiler, run-time system and library
- Implementation is based on imperative stack machine
- Constraint solvers are separate program components
- Constraints are passed at run-time in symbolic form to constraint solvers
- Automatic storage management for data and constraints

Presentation